## Microeconomic Theory II

## Final Exam

Spring 2016
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Carefully explain and support your answers.

Question 1. Consider the following game. First, nature (player 0) selects $t_{1}$ with probability $p, 0<p<1$, or $t_{2}$ with probability $1-p$. Next, player 1 selects $L$ or $R$. Lastly, player 2 selects $U$ or $D$.

(a) Find all pure-strategy weak Perfect Bayesian Nash equilibria of this game. Carefully explain.
(b) Which of the equilibria above satisfy the intuitive criterion? Carefully explain.
(c) How does your answer above in part (a) depend on $p$ ? Carefully explain why this is the case.
(d) Briefly discuss how and when, in general, the existence of some Perfect Bayesian Nash equilibria in signaling games may depend on $p$.

Question 2. Consider a principal-agent model in which the agent chooses between two levels of effort, $\left\{e_{l}, e_{h}\right\}=\{0,1\}$. The principal pays the agent a wage $w_{s}$ in state $s$ and realizes output of $\pi_{s}$. There are four states, with the probability of a state contingent on effort given by:

$$
\begin{array}{ccccc}
\text { effort level } & \pi_{1} & \pi_{2} & \pi_{3} & \pi_{4} \\
e_{l}(=0) & \frac{3}{8} & \frac{3}{8} & \frac{1}{8} & \frac{1}{8} \\
e_{h}(=1) & \frac{1}{4} & \frac{1}{4} & \frac{1}{4} & \frac{1}{4}
\end{array}
$$

The agent's utility function is $\sqrt{w}-e$ and his reservation utility is $\underline{u}=2$. The principal is risk neutral, with utility given by $\pi-w$.
(a) Compute the wage schedule that optimally implements $e_{h}$ when effort is observable.
(b) Compute the wage schedule that optimally implements $e_{h}$ when effort is unobservable.
(c) Consider the wage schedule $\left\{w_{1}, w_{2}, w_{3}, w_{4}\right\}=\{1,1,16,36\}$. Does this wage schedule implement $e_{h}$ ? Does it optimally implement $e_{h}$ ? Explain.

Question 3. Consider a game consisting of two repetitions of the following stage game:


Players observe the outcome of the first stage before playing the second, with payoffs consisting of the sum of the two stages.
(a) Find the pure-strategy subgame-perfect Nash equilibrium that results in the lowest total payoff for the two players. Find the pure-strategy subgameperfect Nash equilibrium that results in the highest total payoff for the two players.
(b) Suppose that the payoffs $(3,3)$ from $(Y, B)$ are replaced by $(4,3)$. How does this change your answers above? Would you expect player 1 to benefit from this increased payoff? Briefly discuss and explain.
(c) Suppose that the payoffs $(3,3)$ from $(Y, B)$ are replaced by $(3,4)$. Would you expect player 2 to benefit from this increased payoff? Briefly discuss and explain.

